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## Food Desert Statistics

Obesity is a big problem in the United States. Studies show that certain racial groups are more affected by obesity than others. These problems may be worse in certain communities because access to affordable and nutritious food is difficult. This is especially true for those living in low-income communities of color and rural areas with limited access to grocery stores. These areas are often called "food deserts."

Residents of food deserts may rely more on convenience stores and fast food restaurants since access to grocery stores is limited. These convenience stores and fast food restaurants don't typically sell the variety of foods needed for a healthy diet such as fresh fruits and vegetables, whole grains, fresh dairy and lean meat products. If they do sell them, they often cost more than they cost at grocery stores. This puts those who live in food deserts at a financial and nutritional disadvantage.

Studies show that:

- Of all U.S. households, 2.3 million ( 2.2 percent) live more than a mile from a supermarket and do not have access to a vehicle. An additional 3.2 percent live between a half-mile to a mile from a supermarket with no vehicle access.
- 23.5 million people live in low-income areas more than one mile from a supermarket.
- Low-income census tracts have half as many supermarkets as wealthy tracts.
- 8 percent of African Americans live in a census tract with a supermarket, compared to 31 percent of whites.
- Low-income zip codes have 30 percent more convenience stores, which tend to lack healthy items, than middle-income zip codes.
- Residents in 20 percent of rural counties live more than 10 miles from a supermarket.
- For every additional supermarket in a census tract, produce consumption increases for 32 percent of African Americans and 11 percent of whites.

[^0]

| Scatter plot fit | Scatter plot fit <br> Card B | Scatter plot fit <br> Card C |
| :---: | :---: | :---: |
| Scatter plot fit <br> Card D | Scatter plot fit <br> Card E | Scatter plot fit |
| Scatter plot fit <br> Card G | Scatter plot fit <br> Card H |  |

## Station E: Are You Ready For More?

1. Students in Charlotte, NC were interested to examine the access in their city. They collected the following data. In this case, they also collected the population within the neighborhood (defined by zip code).

| Population | Median <br> household <br> income (2019) | Organic <br> produce <br> available |
| :---: | :---: | :---: |
| 71048 | 65963 | 27 |
| 59664 | 93942 | 40 |
| 49635 | 59438 | 43 |
| 9280 | 136333 | 44 |
| 53629 | 51676 | 44 |
| 37286 | 91494 | 44 |
| 37309 | 45808 | 46 |
| 11315 | 88039 | 47 |


| Population | Median <br> household <br> income (2019) | Organic <br> produce <br> available |
| :---: | :---: | :---: |
| 11195 | 92786 | 55 |
| 43931 | 52766 | 55 |
| 42263 | 71914 | 55 |
| 19283 | 93938 | 56 |
| 28523 | 90057 | 57 |
| 20317 | 76022 | 58 |
| 47208 | 49465 | 59 |

a. Create a scatter plot for the (median household income, organic produce available) and describe any relationship between the two variables.
b. Compare this relationship to the one you found for San Antonio. What do you think are the reasons for any similarities or differences?

| Population | Median <br> household <br> income (2019) | Organic <br> produce <br> available |
| :---: | :---: | :---: |
| 71048 | 65963 | 27 |
| 59664 | 93942 | 40 |
| 49635 | 59438 | 43 |
| 9280 | 136333 | 44 |
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c. Create a scatter plot for the (population, organic produce available) and describe any relationship between the two variables.
d. One of the points appears to be an outlier. How does your answer to question 3 change if the outlier is removed?
2. Clare, Diego, and Elena collect data on the mass and fuel economy of cars at different dealerships. Clare finds the line of best fit for data she collected for 12 used cars at a used car dealership. The line of best fit is $y=\frac{-9}{1000} x+34.3$, where $x$ is the car's mass, in kilograms, and $\boldsymbol{y}$ is the fuel economy, in miles per gallon.

Diego made a scatter plot for the data he collected for 10 new cars at a different dealership.

Elena made a table for data she collected on 11 hybrid cars at another dealership.
a. Interpret the slope and $y$-intercept of Clare's line of best fit in this situation.

b. Diego looks at the data for new cars and used cars. He claims that the fuel economy of new cars decreases as the mass increases. He also claims that the fuel economy of used cars increases as the mass increases. Do you agree with Diego's claims? Explain your reasoning.
c. Elena looks at the data for hybrid cars and correctly claims that the fuel economy decreases as the mass increases. How could Elena compare this decrease for hybrid cars to the decrease for new cars? Explain your reasoning.

| Mass <br> (kilograms) | Fuel economy <br> (miles per gallon) |
| :---: | :---: |
| 1,100 | 38 |
| 1,200 | 39 |
| 1,250 | 35 |
| 1,300 | 36 |
| 1,400 | 31 |
| 1,600 | 27 |
| 1,650 | 28 |
| 1,700 | 26 |
| 1,800 | 28 |
| 2,000 | 24 |
| 2,050 | 22 |

3. (Technology required.) Priya uses several different ride services to get around her city. The table shows the distance, in miles, she traveled during her last 10 trips and the price of each trip, in dollars.
a. Priya creates a scatter plot of the data using the distance, $x$, and the price, $y$. She determines that a linear model is appropriate to use with the data. Use technology to find the regression equation.
b. Interpret the slope and the $y$-intercept of the line of best fit in this situation.
c. Use the line of best fit to estimate the cost of a 3.6-mile trip. Will this estimate be close to the actual value? Explain your reasoning.

| Distance (miles) | Price (dollars) |
| :---: | :---: |
| 3.1 | 12.5 |
| 4.2 | 14.75 |
| 5 | 16 |
| 3.5 | 13.25 |
| 2.5 | 12 |
| 1 | 9 |
| 0.8 | 8.75 |
| 1.6 | 9.75 |
| 4.3 | 12 |
| 3.3 | 14 |

d. On her next trip, Priya tries a new ride service and travels 3.6 miles, but she pays only $\$ 4.00$ because she receives a discount. Include this trip in the table and calculate the regression equation for the 11 trips. Did the slope of the line of best fit increase, decrease, or stay the same? Why? Explain your reasoning.
e. Priya uses the new ride service for her 12 th trip. She travels 4.1 miles and is charged $\$ 24.75$. How do you think the slope of the regression equation will change when this 12th trip is added to the table?

M1.U4.L7 Best Residuals card sort


M1.U4.L7 Best Residuals card sort

|  |  |
| :---: | :---: |
| For Teacher Demonstration | For Teacher Demonstration |


|  |  |
| :--- | :--- |
| a. The number of ice cream <br> cones sold rises as the <br> temperature outside rises. | d. As the number of people in a <br> family increases, the number <br> of cars the family owns <br> increases. |
| b. The average speed of travel <br> from Mooresville to <br> Carowinds on the interstate <br> increases as the average <br> amount of time it takes <br> decreases. | e. The number of pirates has <br> increased as the global <br> average temperature has <br> increased. ${ }^{1}$ |
| c. The per capita cheese <br> consumption has increased <br> as the number of people who <br> died by getting tangled in their <br> bedsheets has increased. | f. |
| As the divorce rate in Maine <br> increases, so does the per <br> capita consumption of <br> margarine in pounds. ${ }^{3}$ |  |

${ }^{1}$ From http://goopennc.oercommons.org/courses/correlation-and-causation-practice-worksheet/view
${ }^{2}$ From http://tylervigen.com/spurious-correlations
${ }^{3}$ From http://goopennc.oercommons.org/courses/association-and-causation/view

## Modeling Rubric ${ }^{1}$

| Skill | Score |  |  | Notes or Comments |
| :---: | :---: | :---: | :---: | :---: |
|  | Proficient | Developing | Needs Revisiting |  |
| 1. Decide What to Model | - Assumptions made are clearly identified and justified. Resulting limitations are stated when appropriate. <br> - Variables of interest are clearly identified and chosen wisely, and appropriate units of measure are used. | - Assumptions are noted but lacking in justification or difficult to find. <br> - Variables of interest are noted, but may lack justification, be difficult to find, or not be measured with appropriate units. | - No assumptions are stated. <br> - No variables are defined. |  |
|  | To improve at this skill, you could: <br> - Ask questions about the situation to understand it better <br> - Check the assumptions you're making to see if they're reasonable (Try asking a friend, or imagining that you're a person involved in the scenario. Would those assumptions make sense to you?) <br> - Double-check the variables you've identified: Are there other quantities in the situation that could vary? Is there something you've identified as a variable that is actually fixed or determined? (Remember that more abstract things like time and speed are also quantities.) |  |  |  |
| 2. Formulate a Mathematic al Model | - An appropriate model is chosen and represented clearly. <br> - Diagrams, graphs, etc. are clear and appropriately labeled. | Parts of the model are unclear, incomplete, or contain mistakes. | No model is presented, or the presentation contains significant errors. |  |

To improve at this skill, you could:

- Check your model more carefully to make sure it really fits well
- Consider a wider variety of possible models, to find one that fits the situation better
- Think about the situation more deeply before trying to find a model
- Convince a skeptic: Pretend that you think your model is inadequate, or ask a friend to pretend to be skeptical of it. What would a skeptic find wrong with your model? Try to fix those things, or explain why they're not actually problems.

[^1]| Skill | Score |  |  |  | Notes or Comments |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Proficient |  |  | Developing | Needs Revisiting |

## Modeling Prompt 3A

A homeowner wants to replace their old heating system. Energy is measured in kilowatt-hours (kWh). It takes about $11,700 \mathrm{kWh}$ of energy to heat the house for the winter. The current heating system uses natural gas and is $60 \%$ efficient, which means that for every 100 kWh of natural gas it uses, it produces 60 kWh of heat. With the homeowner's current system, it costs $\$ 975$ to heat the house.

Research at least two other options available in your area that this homeowner could replace their heating system with. Assume that natural gas costs $\$ 0.05 / \mathrm{kWh}$ and electricity costs $\$ 0.21 / \mathrm{kWh}$. The house is 2,500 square feet.

The homeowner also has an air conditioner that uses $2,500 \mathrm{kWh}$ of electricity per year and produces 290 kWh of cooling for every 100 kWh it uses. They also have a water heater that uses $4,300 \mathrm{kWh}$ of electricity per year and produces 90 kWh of heat for every 100 kWh it uses. These systems could also be replaced if there is a cheaper option, but it isn't necessary.

1. Which system would you recommend? Make a graph to convince the homeowner to switch to this system.
2. If the homeowner switches to the system you recommend, how long will it take them to save as much money as the new system cost?

## Modeling Prompt 3B

A homeowner wants to replace their old heating system. Energy is measured in kilowatt-hours (kWh). It takes about $11,700 \mathrm{kWh}$ of energy to heat the house for the winter. The current heating system uses natural gas and is $60 \%$ efficient, which means that for every 100 kWh of natural gas it uses, it produces 60 kWh of heat. With the homeowner's current system, it costs $\$ 975$ to heat the house. Assume that natural gas costs $\$ 0.05 / \mathrm{kWh}$ and electricity costs $\$ 0.21 / \mathrm{kWh}$.

The homeowner also has an air conditioner that uses $2,500 \mathrm{kWh}$ of electricity per year and produces 290 kWh of cooling for every 100 kWh it uses. They also have a water heater that uses $4,300 \mathrm{kWh}$ of electricity per year and produces 90 kWh of heat for every 100 kWh it uses. These systems could also be replaced if there is a cheaper option, but it isn't necessary.

Here are three other types of heating systems the homeowner could replace their current system with:

- A new furnace which also runs on natural gas and is more efficient. For every 100 kWh of natural gas it uses, it produces 95 kWh of heat. This system costs $\$ 5,000$ to install.
- A geothermal heat pump. This system uses electricity instead of natural gas, but it produces 4 kWh of heat for every 1 kWh of electricity it uses. It costs $\$ 14,000$, but it's very low-maintenance and it also replaces the air conditioner and water heater.
- A grid-tied solar array. This system is connected to the electrical grid so that when it generates more energy than the house needs, the extra electricity can be sold back to the grid. Over the whole year, the house will use as much electricity as is sold back, which means the homeowner would basically be heating and cooling the house for free. It costs $\$ 16,000$ to install.

1. Which system would you recommend? Make a graph to convince the homeowner to switch to this system.
2. How long will it take to save as much money as the new system cost?

## Modeling Prompt 4A

1. Below are the characteristics of colleges that we have data about. Choose two that might be related. What do you predict the relationship between them is?

- college ownership: public, private non-profit, or private for-profit
- average SAT score of admitted students
- acceptance rate
- number of enrolled students
- average cost of attendance per year
- median earnings 10 years after graduation
- highest degree awarded
- completion rate
- percent of students who self-identify as white
- median ACT score of admitted students

2. Take a look at the data in the spreadsheet. Before calculating, do some estimation based on the data. Can you tell if your hypothesis seems reasonable?
3. Use an appropriate display to summarize the data.
4. Analyze your graph or table and do any other calculations needed. Do your results confirm your prediction? If not, what do you think explains the results?
5. Here are some headlines. What analysis do you think the article describes? Give some examples of evidence that would support the headline or contradict it.

- "Students from Selective Colleges Tend to Succeed"
- "Isolation at Larger Colleges Leads to Higher Dropout Rates"
- "High Cost of Private Colleges Not Outweighed by Lifetime Earnings"


## Modeling Prompt 4B

1. Below are the characteristics of colleges that we have data about. Choose two that might be related. What do you predict the relationship between them is?

- college ownership: public, private non-profit, or private for-profit
- average SAT score of admitted students
- acceptance rate
- number of enrolled students
- average cost of attendance per year
- median earnings 10 years after graduation

2. Take a look at the data in the spreadsheet. Before calculating, do some estimation based on the data. Can you tell if your hypothesis seems reasonable?
3. Use an appropriate display to summarize the data.
4. Analyze your graph or table and do any other calculations needed. Do your results confirm your prediction? If not, what do you think explains the results?
5. Here are some headlines. What analysis do you think the article describes? Give some examples of evidence that would support the headline or contradict it.

- "Students from Selective Colleges Tend to Succeed"
- "Isolation at Larger Colleges Leads to Higher Dropout Rates"
- "High Cost of Private Colleges Not Outweighed by Lifetime Earnings"

Name:
Period:
Date:

## End-of-Unit 4 Student Survey

1. Ending this unit I feel ... (this question could be answered with pictures, words, etc.)
2. How much did you know about the content of this unit before starting?
a. A great deal
b. A little
c. Not much

Feel free to share more:
3. After finishing the unit did your knowledge in the content:
a. Increase greatly
b. Increase a little
c. Stay the Same

Feel free to share more:
4. What was most frustrating for you while learning during this unit?
a. Materials Used
b. Teacher strategies
c. Technology
d. Other: $\qquad$

Feel free to share more:
5. What boosted your confidence in math during this unit?
a. Materials Used
b. Teacher strategies
c. Technology
d. Other: $\qquad$

Feel free to share more:
6. What connections do you think the concepts from this unit make to the world around you?
7. What did your level of engagement and participation during the unit tell you about yourself and the way you see yourself and your abilities in math?
8. How would you like to improve in the next unit?
9. How can your teacher support your goals for improvement in the next unit?
10. I'd like my Math 1 teacher(s) to know that I want them to continue $\qquad$
11. Please share anything else you'd like regarding your experiences in this unit and your feelings about the upcoming unit.


[^0]:    Sources:
    "Access to Affordable and Nutritious Food: Measuring and Understanding Food Deserts and their Consequences:" Report (2009) to Congress from the United States Department of Agriculture.
    "The Grocery Gap: Who Has Access to Healthy Food and Why It Matters:" Report from Policy Link and the Food Trust.

[^1]:    ${ }^{1}$ Adapted from IM 9-12 Math Algebra 1 Modeling Prompts https://curriculum.illustrativemathematics.org/HS/teachers/index.html, copyright 2019 by Illustrative Mathematics. Licensed under the Creative Commons Attribution 4.0 license https://creativecommons.org/licenses/by/4.0/.

